

Generation of multiple sound zones by spatial filtering in wavenumber domain using a linear array of loudspeakers

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Introduction

■ Generation of acoustically bright and dark zones using an array of loudspeakers

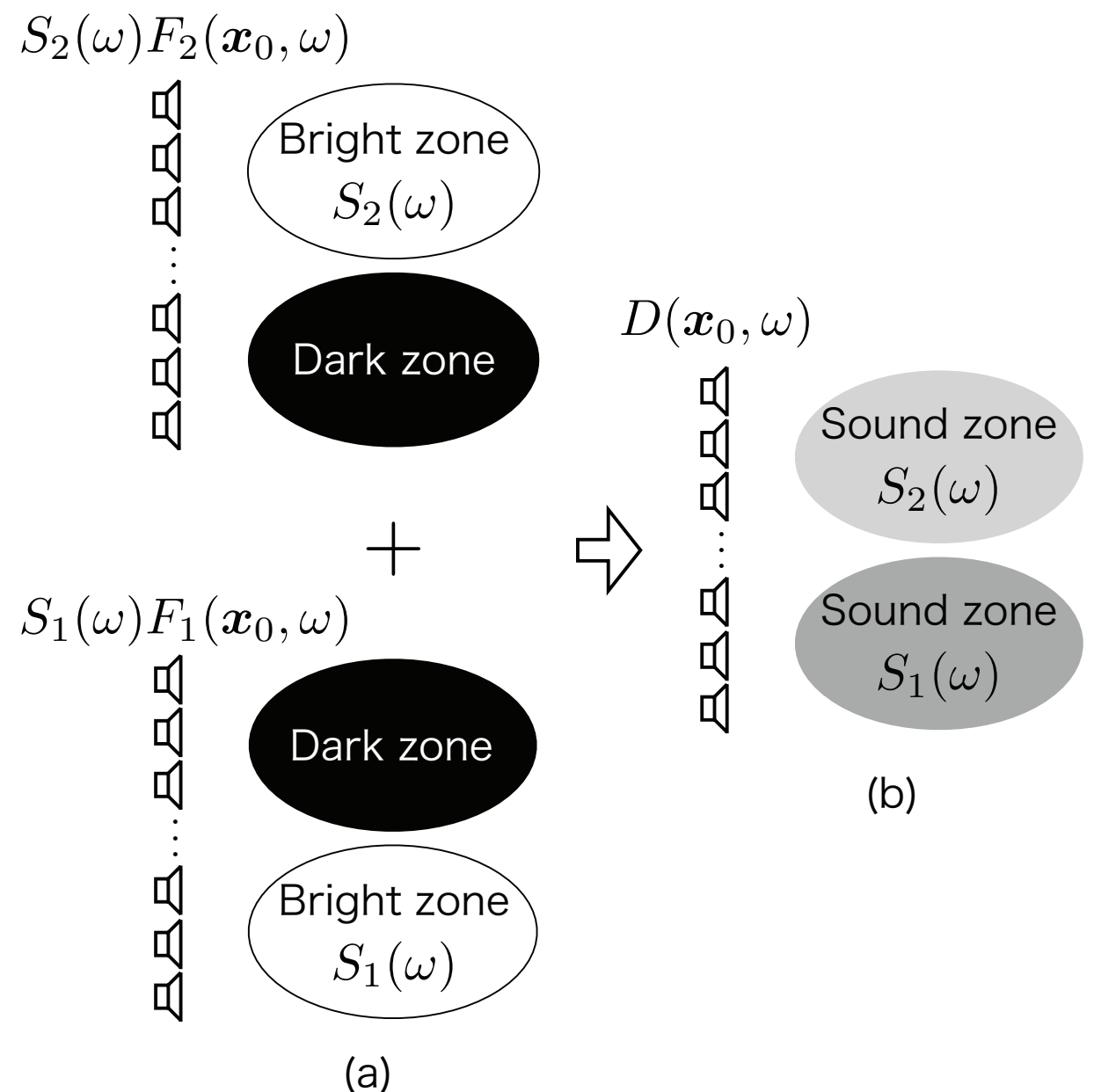
■ (a) generating bright and dark zones

■ (b) multiple spots generation

■ Applications

- ✱ Personal audio system
- ✱ Multiple-language guide system
- ✱ Virtual reality applications

without headphone



Previous methods and their problems

■ Most methods based on multiple points control

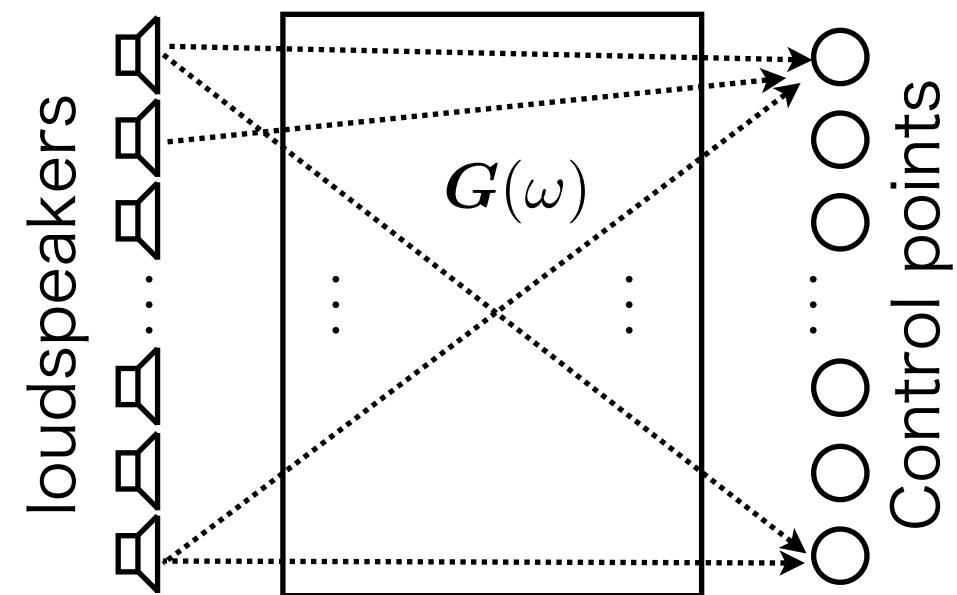
■ Principle

(e.g. J.-W. Choi *et al.* in *JASA*, 2002.)

- ✱ Numerical calculation of the inverse of the spatial correlation matrix

■ Problems

- ✱ Quite unstable
- ✱ Iterative calculation for deciding regularization parameter



■ Energy difference maximization (EDM)

■ Principle

(M. Shin *et al.* in *JASA*, 2010.)

- ✱ Numerical calculation of the eigenvector of the spatial correlation matrix

■ Problem

- ✱ Iterative calculation for deciding tuning factor

Novel approach

Problems of conventional methods

- Unstable
- Iterative calculation

3 characteristics of proposed method

- Analytically derived stable filters
- No iterative calculation
- Implemented by using actual 64 loudspeakers

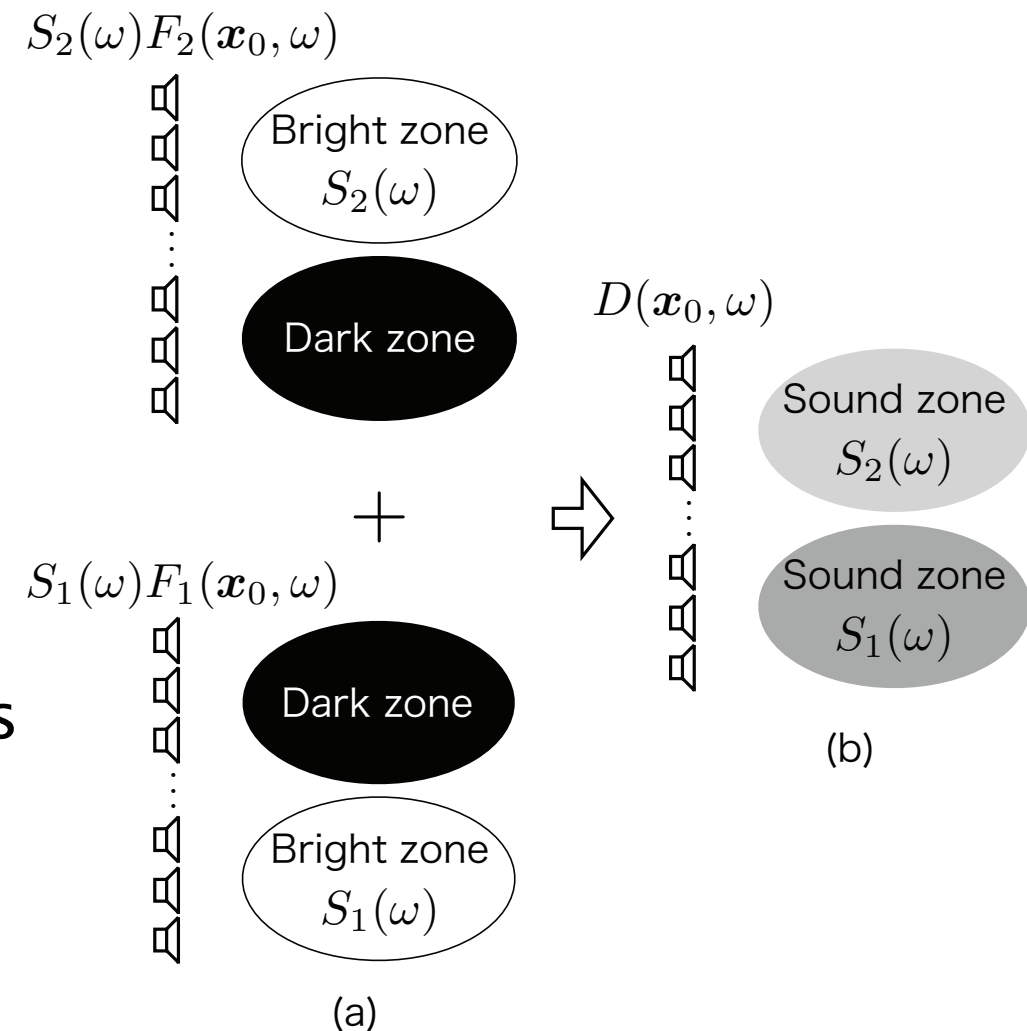
Nomenclature

- Sound source signal : $S(\omega)$
- Driving signals of loudspeakers
 - (a) Generating bright and dark zone

$$D(\mathbf{x}_0, \omega) = S_1(\omega) F_1(\mathbf{x}_0, \omega)$$

- (b) Generating multiple sound zones

$$D(\mathbf{x}_0, \omega) = \sum_{i=1}^M S_i(\omega) F_i(\mathbf{x}_0, \omega)$$



How to calculate?

Basic theory

- Spectral division method (SDM) (J. Ahrens *et al.* in *IEEE ASLP.*, 2010.)
 - Sound field reproduction using planer or linear arrays of loudspeakers
 - ✱ Driving signals of secondary sources are analytically derived

- ✱ Acoustical single layer potential in a plane

$$P(\mathbf{x}, \omega) = \int_{-\infty}^{\infty} D(\mathbf{x}_0, \omega) G_{3D}(\mathbf{x} - \mathbf{x}_0, \omega) d\mathbf{x}_0$$

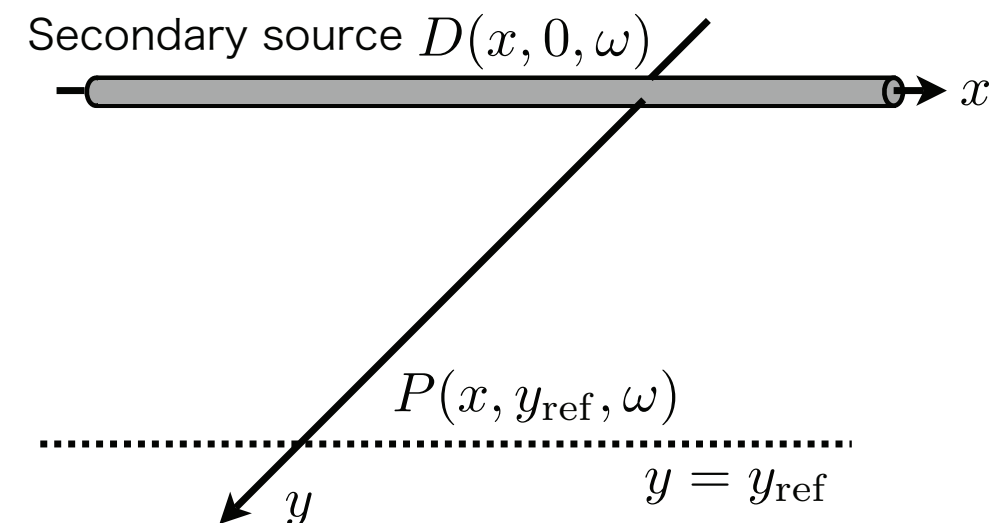
- ✱ Spatial Fourier transform along with x -axis

$$\tilde{P}(k_x, y, \omega) = \tilde{D}(k_x, \omega) \cdot \tilde{G}(k_x, y, \omega)$$

- ✱ Driving signals of secondary sources

$$\tilde{D}(k_x, \omega) = \frac{\tilde{P}(k_x, y_{\text{ref}}, \omega)}{\tilde{G}(k_x, y_{\text{ref}}, \omega)} \quad \boxed{\mathcal{F}_x^{-1}} \quad D(x, \omega) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \frac{\tilde{P}(k_x, y_{\text{ref}}, \omega)}{\tilde{G}(k_x, y_{\text{ref}}, \omega)} e^{-jk_x x} dk_x$$

- ✱ Driving signals in each wavenumber domain is completely orthogonal each other and much stable rather than multiple points control



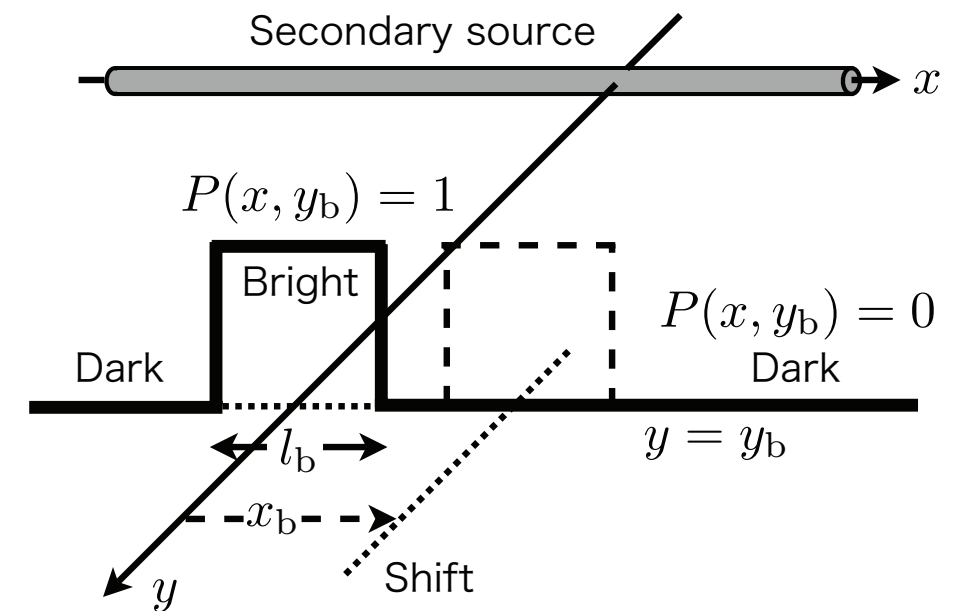
Proposed method

■ Analytically derived spatial filters in wavenumber domain

■ Spatial filters in wavenumber domain

$$\tilde{F}(k_x, \omega) = \frac{\tilde{P}(k_x, y_{\text{ref}}, \omega)}{\tilde{G}(k_x, y_{\text{ref}}, \omega)}$$

$$\left. \begin{array}{l} P(x, y_{\text{ref}}, \omega) = 1 \\ P(x, y_{\text{ref}}, \omega) = 0 \end{array} \right\} \begin{array}{l} \text{Modeled by} \\ \text{Rectangular window} \end{array}$$



$$P(x, y_b) = \Pi \left(\frac{x}{l_b} \right) = \begin{cases} 1, & \text{for } |x| \leq l_b/2 \\ 0, & \text{elsewhere} \end{cases} \xrightarrow{\mathcal{F}_x} \tilde{P}(k_x) = l_b \operatorname{sinc} \left(\frac{k_x l_b}{2\pi} \right)$$

✱ Shift theorem introduced to shift rectangular window along with x -axis

$$\tilde{P}_{\text{shift}}(k_x) = \tilde{P}(k_x) \exp(jk_x x_b) = l_b \operatorname{sinc} \left(\frac{k_x l_b}{2\pi} \right) \exp(jk_x x_b)$$

✱ Spatial filters for generating bright and dark zones

$$\tilde{F}(k_x, \omega) = \frac{l_b \operatorname{sinc} (k_x l_b / 2\pi) \exp(jk_x x_b)}{\tilde{G}(k_x, y_b, \omega)}$$

Arbitrary length : l_b
Arbitrary position : $[x_b, y_b]^T$

Computer simulations

Simulation condition

- Speed of sound : 343.25 m/s
- distance between adjacent loudspeakers : 0.05 m
- Tuning factor for EDM : 0.9999

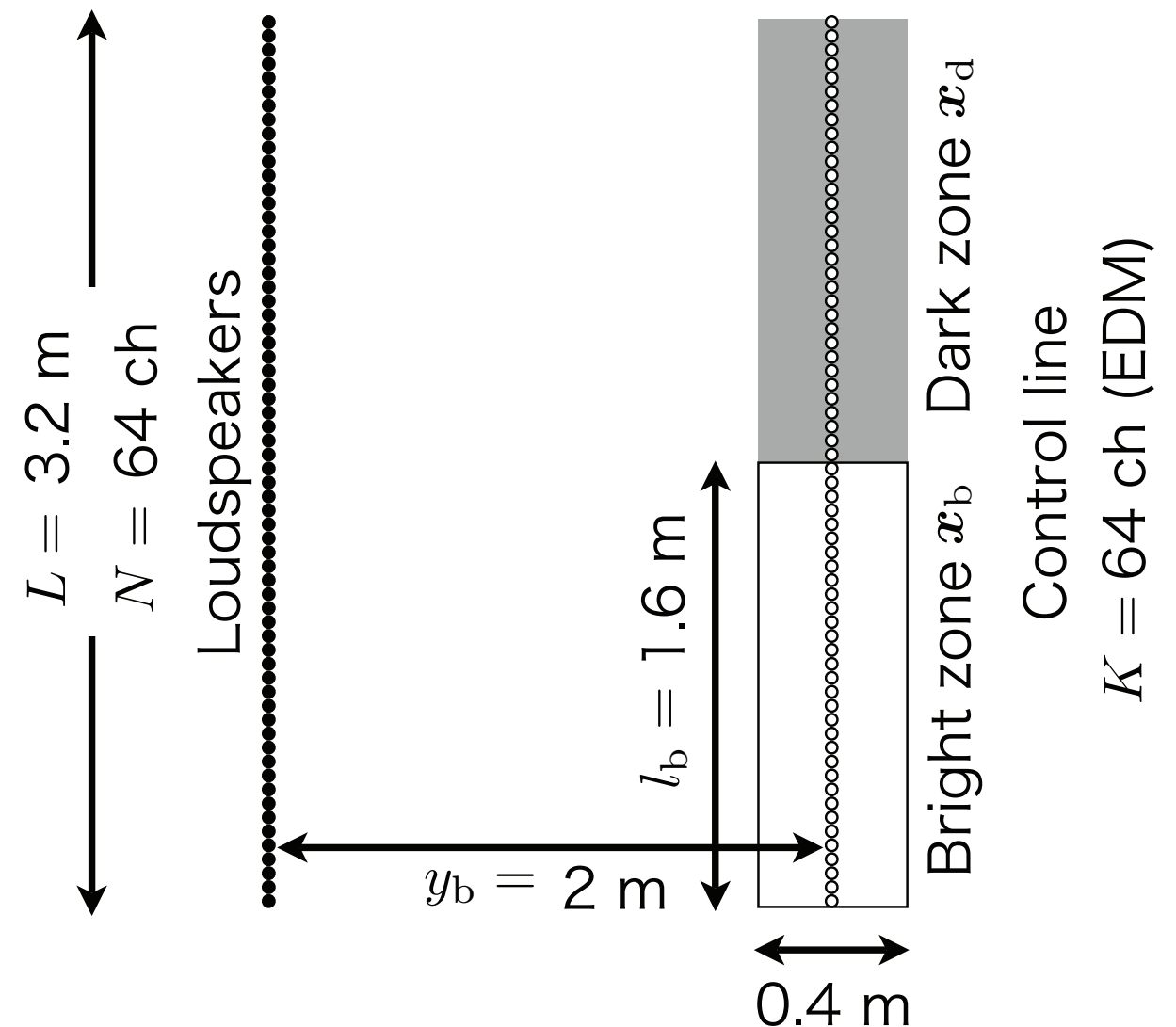
Evaluation values

- Sound pressure level

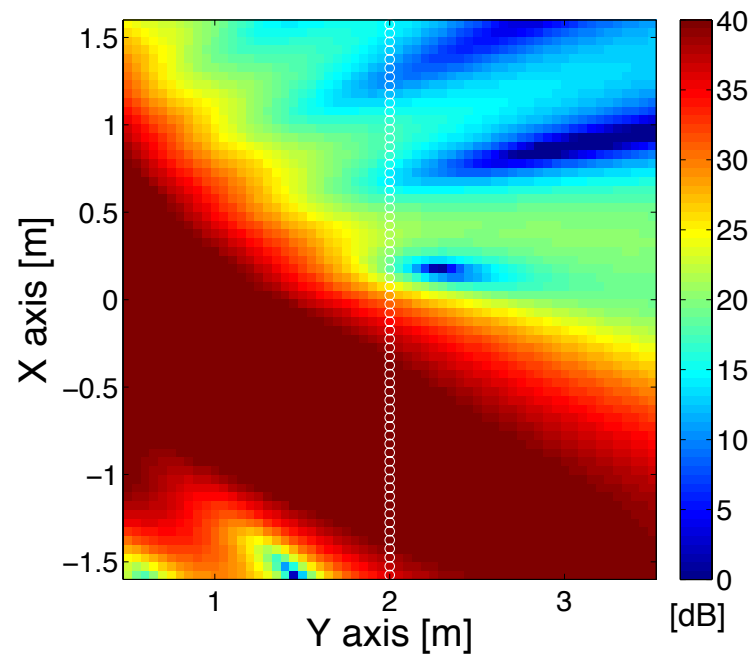
$$P_{\text{SPL}}(\mathbf{x}, \omega) = 10 \log_{10} \left| \hat{P}(\mathbf{x}, \omega) \right|^2$$

- Bright to dark ratio

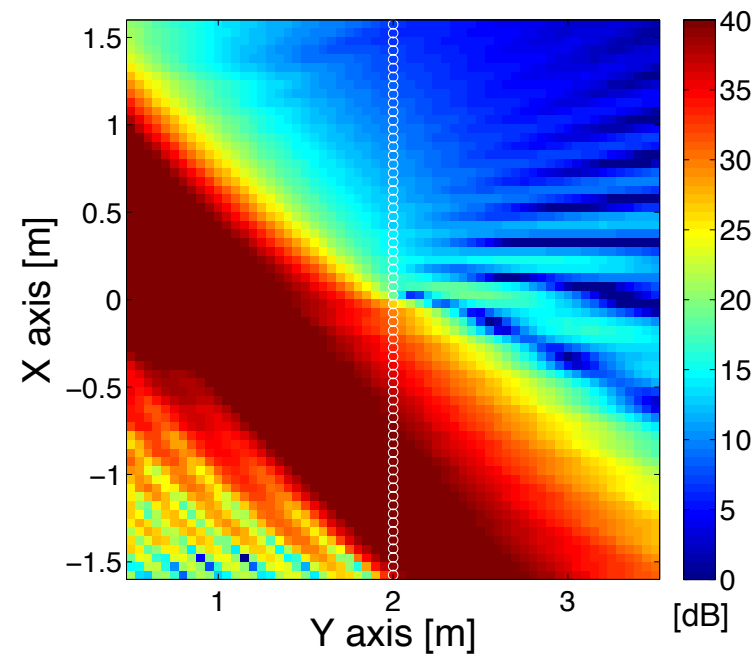
$$BDR(\omega) = 10 \log_{10} \frac{\sum_{\mathbf{x}_b} \left| \hat{P}(\mathbf{x}_b, \omega) \right|^2}{\sum_{\mathbf{x}_d} \left| \hat{P}(\mathbf{x}_d, \omega) \right|^2}$$



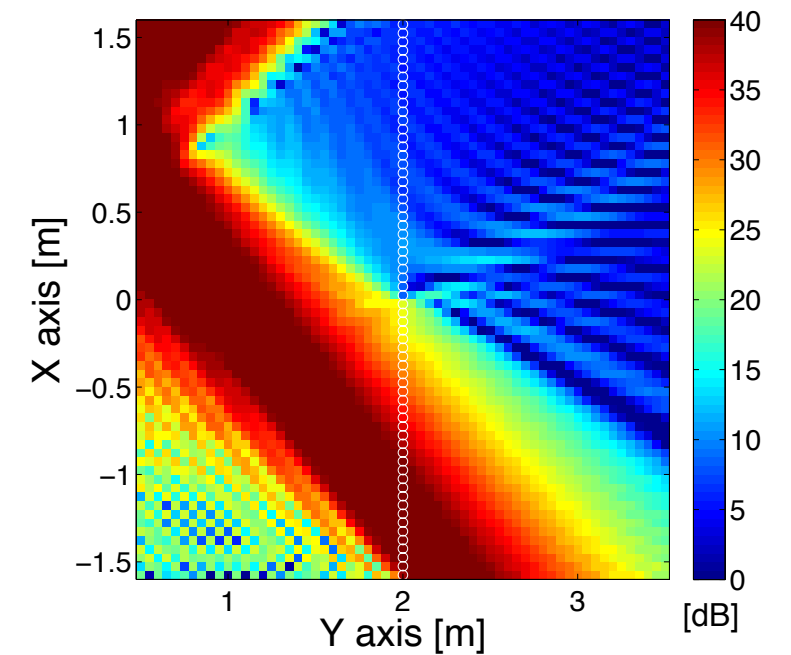
Simulation results : $P_{\text{SPL}}(x)$



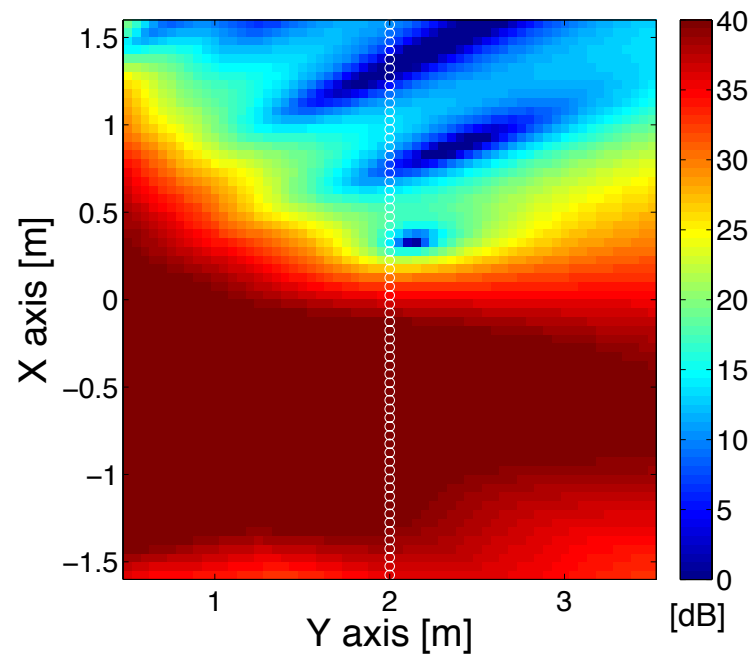
EDM (500 Hz)



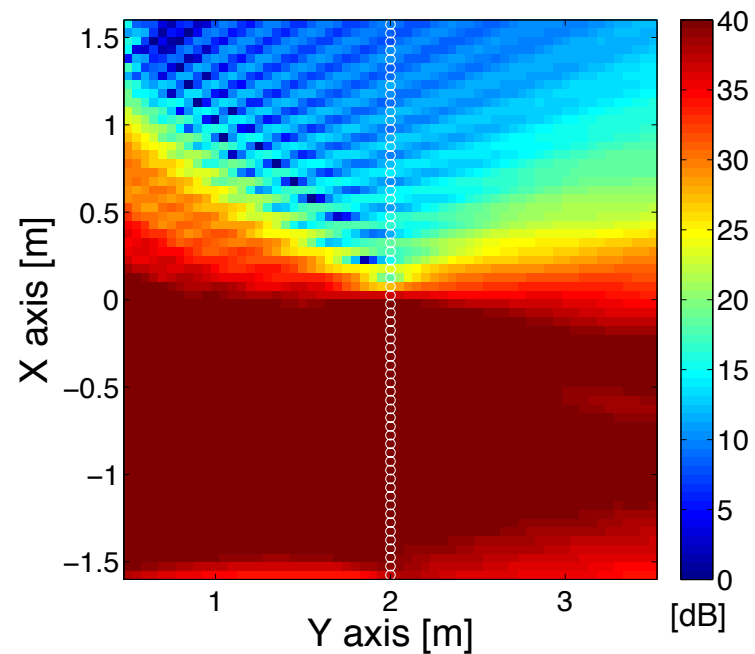
EDM (2 kHz)



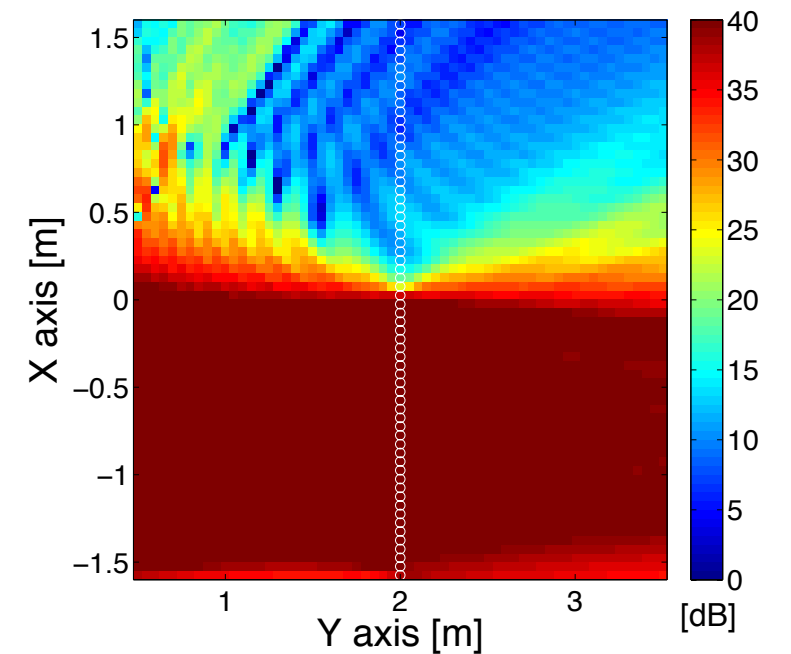
EDM (5 kHz)



Proposed (500 Hz)

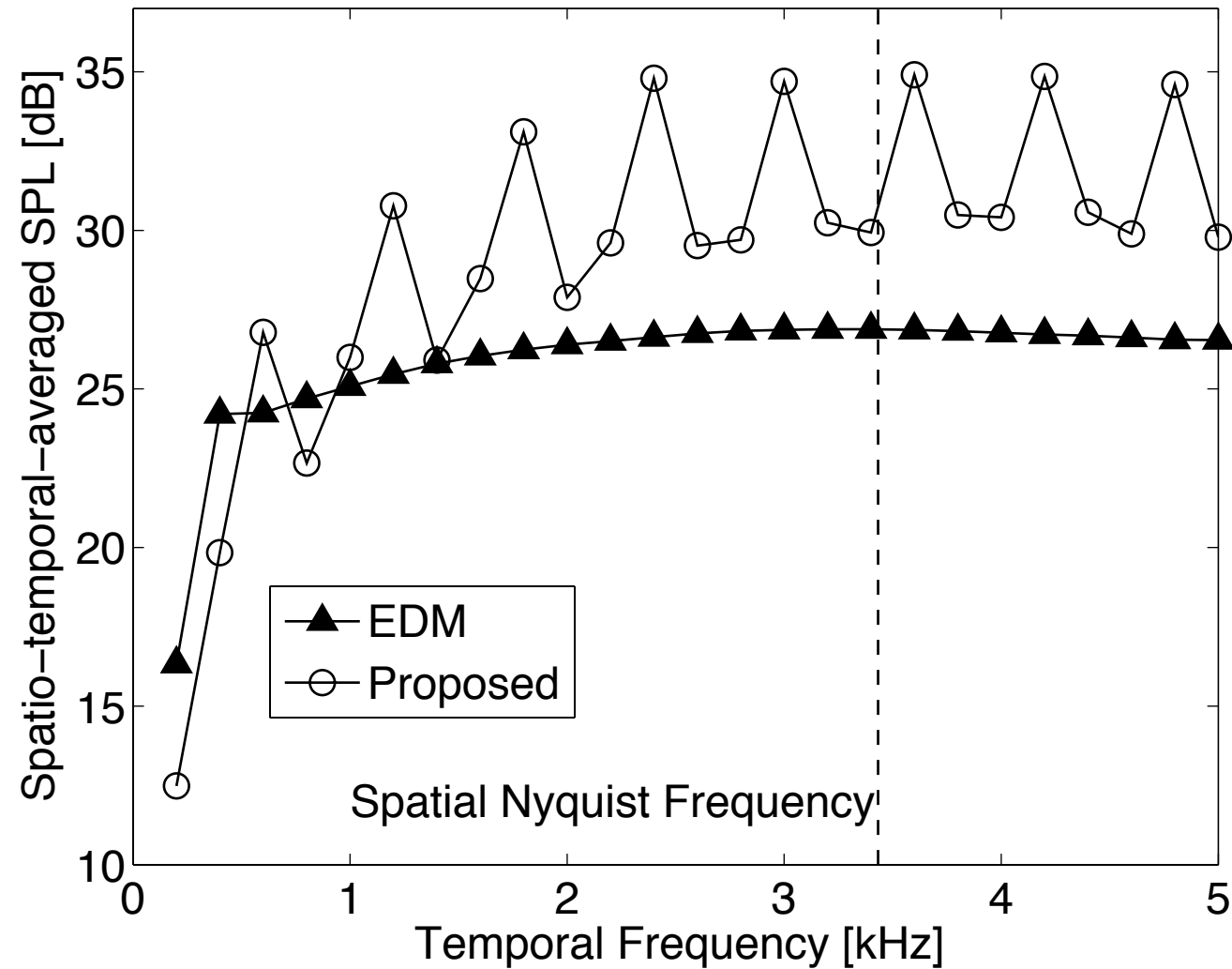


Proposed (2 kHz)



Proposed (5 kHz)

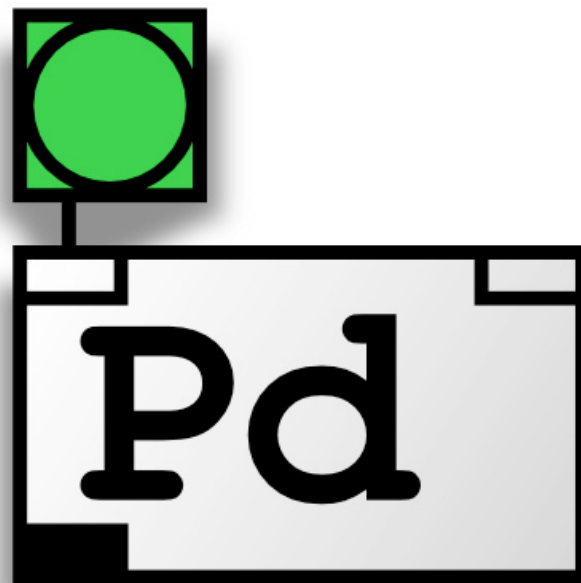
Simulation results : BDR



$$BDR(\omega) = 10\log_{10} \frac{\sum \mathbf{x}_b \left| \hat{P}(\mathbf{x}_b, \omega) \right|^2}{\sum \mathbf{x}_d \left| \hat{P}(\mathbf{x}_d, \omega) \right|^2}$$

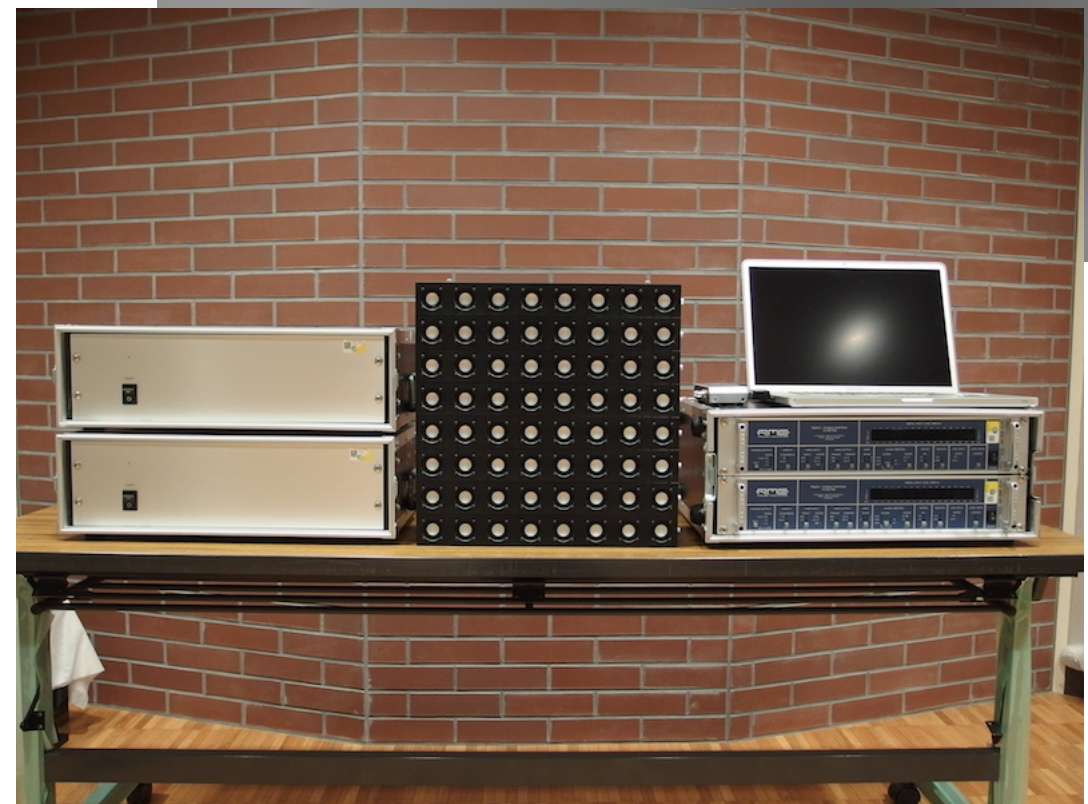
DEMO 1

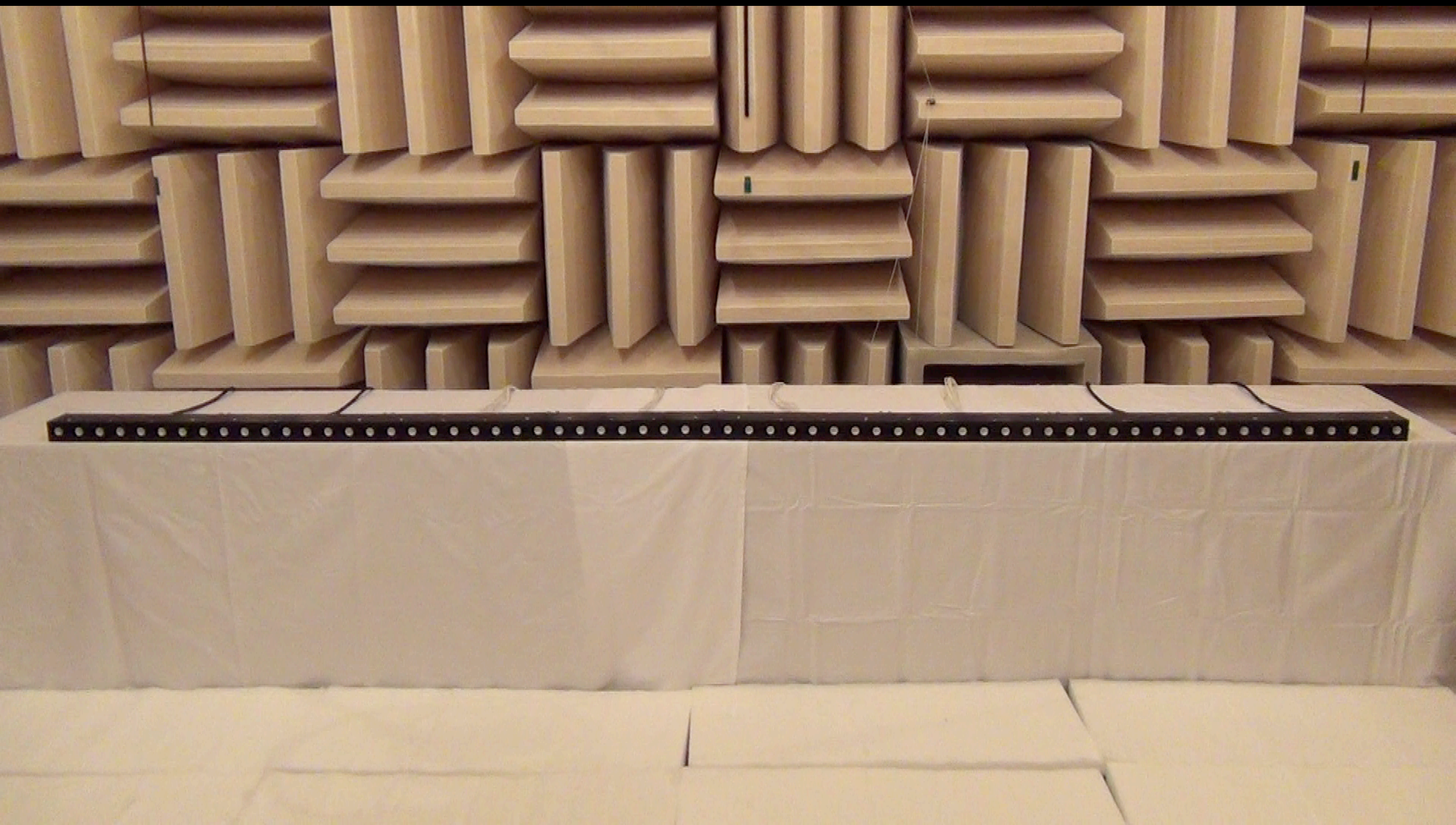
implemented by PureData



DEMO 2

implemented by actual linear array of loudspeakers





Concluding remarks

- Acoustically bright zone or multi-zones generation using loudspeakers
 - Analytically derived stable filters
 - No iterative calculation
 - Implemented by using an actual linear array of 64 loudspeakers

Grazie mille!!

■ Acknowledgement

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